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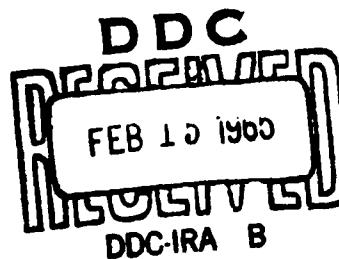
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## **HYDRONAUTICS, incorporated research in hydrodynamics**

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TECHNICAL REPORT 233-6

HIGH FREQUENCY FATIGUE OF METALS  
AND THEIR CAVITATION  
DAMAGE RESISTANCE

By

A. Thiruvengadam

December 1964

Prepared Under

Office of Naval Research  
Department of the Navy  
Contract No. Nonr-3755(00) FBM  
NR 062-293

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## NOTATION

$Q$	Quality factor
$f_n$	Natural frequency
$\Delta f$	Width of the resonance curve at half the maximum amplitude
$\lambda$	Wave length of sound
$c$	Velocity of sound
$E$	Modulus of elasticity
$\rho$	Density
$\eta$	Fatigue notch sensitivity
$K_f$	Ratio of unnotched fatigue strength to notched fatigue strength
$K_t$	Theoretical stress concentration factor
$\epsilon_{max}$	Maximum strain
$\xi_{max}$	Maximum amplitude
$\sigma_a$	Stress amplitude
$S_e$	Strain energy
$\sigma$	True stress
$\epsilon_p$	True plastic strain
$n$	Strain hardening exponent
$\epsilon_f$	True ultimate fracture strain
$\sigma_f$	True ultimate fracture stress
$\sigma_f'$	Auxiliary true ultimate fracture stress

SUMMARY

Recent experiments (1,2) have shown that the plastic strain energy (as given by the area of the stress-strain diagram obtained from a simple tensile test) is at present the most significant criterion for cavitation damage resistance of metals. Since the strain rates involved in the cavitation damage process were several orders of magnitude higher than that in a simple tensile test from which the strain energy was derived, the above result is surprising.

In order to confirm the preceding result, high frequency fatigue tests at 14.2 kcs (at the same frequency used for cavitation damage tests) were conducted for five metals. Recently Morrow (3) used plastic strain energy as a criterion for finite fatigue life and derived a relationship connecting stress to fracture and number of cycles to fracture by making use of true ultimate tensile strength and the strain hardening exponent. He showed reasonable correlation with forty sets of data. Good correlation is also obtained with the present experiments and Morrow's theory if the strain hardening exponent is reduced by about fifteen percent for all the five metals. This result confirms that plastic strain energy is a good criterion even at high strain rates.

Another result revealed by the present study is the influence of corrosion. Recently (7) it was shown that cavitation damage in a corrosive environment increases greatly while the contributions from direct electrochemical corrosion could not

account for this great increase. It was postulated that the increased damage must come principally from the deterioration of the strength due to corrosion fatigue, but there were serious doubts whether corrosion could play any significant role at these high frequencies. Present experiments show that fatigue strength can be reduced significantly for SAE 1020 steel in 3 percent NaCl solution even at high frequencies, thus confirming the earlier speculations.

#### INTRODUCTION

Recent attempts to characterize the cavitation damage resistance of metals by a common mechanical property have shown that the most significant correlation could be established with the strain energy of the material in the steady state zone (1,2). This strain energy is given by the fracture energy per unit volume of the metal as obtained from the area of the stress-strain diagram from a simple tensile test. The cavitation damage process takes place at strain rates several orders of magnitude higher than the simple tensile test which gives the fracture energy at relatively low strain rates. It seemed surprising that the fracture energy at such low strain rates could still represent the energy absorbing capacity of metals under the highly transient stresses produced by the cavitation bubble collapse. Some experimental verification was needed to clarify the strain rate effects on fracture energy of metals in order to explain these results.

During these studies the thought provoking investigations of Morrow (3) using plastic strain energy as a criterion for finite fatigue life came to the attention of the author. Morrow successfully related the plastic strain energy per cycle to the static true strain energy for forty sets of data including carbon steels, alloy steels, nickel based alloys, various aluminum alloys, beryllium and brass. This prompted the present investigations in which the fatigue tests at a frequency of 14 kcs were conducted following the pioneering work of Gaines (4), Mason (5) and Neppiras (6). Morrow's analysis was extended to the high frequency fatigue tests to see how much the strain rate effects interact and modify the analysis. As a result of this analysis, it has been found that a good correlation between the theory and experiments can be obtained if the value of the strain hardening exponents are reduced by 15 percent from the static result. This shows that the strain rate effects are relatively small when energy is used as a criterion for the fracture mechanism.

Another important aspect clarified by these investigations is the interaction of the corrosive environment on cavitation damage. It has been observed that the damage rates in a corrosive environment are much higher than those observed in a relatively non-corrosive environment (7). The electrochemical corrosion estimated by four different methods could not account for this increase in rate of damage. On the basis of these findings, it was postulated that the major contribution to the increase of rate of damage in a corrosive environment should

come mainly from the change in the fatigue properties of the material in that corrosive environment. However, a popular point of view has hypothesized that under cavitation conditions the surface material was being removed so rapidly that there was insufficient time for appreciable corrosive weakening of the surface. The present investigations include the test results for one metal (1020 SAE steel) in 3 percent NaCl solution and these results show that fatigue properties of non-resistant metal in a corrosive environment can be drastically changed even under very high frequencies.

#### EXPERIMENTAL APPARATUS

The experimental technique adopted for the present investigations consists of oscillating a metallic rod at its resonant longitudinal frequency. This frequency was selected to be the same as that used for previous cavitation damage tests. This technique enables the utilization of the magnetostriction apparatus used previously for cavitation damage tests. Gaines (4) who introduced the idea of using magnetostriction oscillators for cavitation damage testing also suggested the use of the same equipment for fatigue testing as well. He, in fact, carried out a few fatigue tests in his apparatus. However, this technique did not gain popularity until Mason (5) and Neppiras (6) successfully used exponential and stepped velocity transformers, thereby making the technique more versatile, because high strains can be produced on any metal with moderate power. A detailed discussion of the various aspects involved in this method is given by Neppiras (6, 8).

In essence, the apparatus consists of a magnetostriiction transducer, an oscillator, an amplifier, a power supply, a voice coil, an oscilloscope and a frequency counter (Figure 1). An exponential velocity transformer is attached to the magnetostrictive nickel transducer stack. The characteristics of the entire system are shown in Figure 2 for three resonant frequencies. The resonant frequency of the system can be varied by varying the length of that portion of the velocity transformer from the nodal support to the free end by means of extension rods. The amplitude is monitored by a suitable voltage pick-up coil located approximately midway between the node and the antinode. A permanent magnet is used in the immediate vicinity of the coil to increase the induced voltage. This induced voltage is proportional to the displacement amplitude and the instrument is calibrated by measuring the displacement at the antinode with a filar microscope. The accuracy of these measurements is discussed later.

A detailed study of the transducer system showed that the best quality factor was obtained at 14.2 kcs and hence this frequency was selected for fatigue tests. The quality factor is defined as the ratio of usable energy stored in the system to the total input energy and is given by (9),

$$Q = \frac{\sqrt{3}}{\pi} \frac{f_n}{\Delta f} \quad [1]$$

where  $f_n$  is the resonant frequency and  $\Delta f$  is the width of the resonant curve at half of the maximum amplitude.

## DESIGN OF TEST SPECIMENS

General Aspects

The basic principle of the design of the high frequency fatigue specimens is as follows: When a longitudinal vibration of a half wave length of a metallic rod is produced by means of an oscillator, the maximum strain is produced at the node while the maximum velocity and displacement are produced at the antinodes at either end of the rod (Figure 3). If a notch is produced at the node, then the strain is further amplified at the node. It is necessary to amplify the strains by means of a notch because of the power limitations of the driving oscillator. There are two other unwanted side effects due to this notch, namely: (i) the fatigue notch sensitivity and (ii) the change in resonant frequency. These two effects will be discussed subsequently.

The main idea is to attach a half wave length of the metallic rod to the free end of the exponential horn and to vibrate it at the best frequency selected from considerations of the quality factor. The half wave length can be experimentally determined by adjusting the rod length to resonate at the best frequency. An accurate determination of this length and frequency will give the value of velocity of sound for each of the metals tested by the relationship

$$-\lambda f_n = c \quad [2]$$

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where

$\lambda$  is the wave length,

$f_n$  is the resonant frequency, and

$c$  is the velocity of sound.

The modulus of elasticity also can be calculated after determining the density of the metals by the conventional water displacement method, by

$$E = \rho c^2 \quad [3]$$

where

$E$  is the modulus of elasticity

$\rho$  is the density of the metal.

Table 1 gives the physical properties thus determined for each of the six metals under investigation.

Notch Sensitivity

As pointed out earlier, a notch was provided at the node to induce the required strains. It is known that  $f_n$  is sensitive to notches depending upon the geometry of the notches. This effect is characterized by a factor  $\eta$  known as notch sensitivity

$$\eta = \frac{K_f - 1}{K_t - 1} \quad [4]$$

where

$$K_f = \frac{\text{un-notched fatigue strength}}{\text{notched fatigue strength}}, \text{ and}$$

$K_t$  = the theoretical stress concentration factor.

Experimental information on  $\eta$  as a function of notch radius is available for steels and aluminum alloys in References 10 and 11. The notch radius was selected so that  $\eta$  would be as close to unity as possible. The same notch radius was adopted for both Tobin Bronze and Monel since no experimental data were readily available for these metals. Next, the theoretical stress concentration factors for round bars may be found from Reference 12. The dimensions of the notch selected are shown in Figure 4(a). A photograph of the 1020 SAE steel specimen is shown in Figure 4(b).

The stresses are calculated as follows: The maximum strain at the node for a uniform rod in sinusoidal vibration is given by

$$\epsilon_{\max} = \frac{2\pi \xi_{\max}}{\lambda} \quad [5]$$

where  $\xi_{\max}$  is the maximum amplitude. The stress amplitude  $\sigma_a$  is given by

$$\sigma_a = \epsilon_{\max} \cdot E \quad [6]$$

For the present design, the theoretical stress concentration factor from Reference 12 is 1.65 and the area ratio is 4. Hence the magnification factor,  $M$  is 4 times 1.65 and the stress amplitude is given by

$$\sigma_a = 6.6 \frac{2\pi}{\lambda} \xi_{\max} \cdot E \quad [7]$$

#### Effect of Notch on Resonant Frequency

Another effect of the notch is to lower the resonant frequency slightly. This can be rectified by reducing the length of the fatigue specimen after a few trial and error experiments. This modified length can also be predicted by an approximate theory following Neppiras (6). However, the change in wave length due to the notch remains within 10 percent as shown in Table 1 and this can be taken into account in the calculation of stresses.

#### EXPERIMENTAL PROCEDURE AND ACCURACY

##### Amplitude Measurement and Determination of Maximum Stress

As pointed out earlier, the maximum amplitude at the anti-node where the fatigue specimen is attached is monitored by means of a calibrated voice coil located as shown in Figure 1. Since the fatigue specimen forms a half wave length, its addition does not change either the frequency or the calibration. The voltage developed by the coil was of the order of 35 volts, corresponding to an amplitude of  $2.5 \times 10^{-3}$  inch and hence

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maintain constant amplitude. (An automatic amplitude control has been designed for future studies). The determination of this fracture time is no problem especially above ten million cycles since it would take about 12 minutes to reach this value. It would take 20 hours to reach a billion cycles and this time is designated as "run-out" time. (Run-out is defined as the number of cycles at which the test is discontinued even if the specimen does not fracture).

Fabrication of Test Pieces

Figure 4(a) shows the dimensional tolerances required for the fabrication of the specimens. The specimens were ground to the final dimensions from a 3/4 inch round bar stock for all the five metals except for SAE 1020 steel. The specimens were in the annealed condition and of the same heat as was used for previous cavitation damage tests and stress-strain measurements. Cavitation damage specimens and tensile test specimens were prepared from the same bar stock of the metals. The fatigue specimens for SAE 1020 steel were prepared from 1/2 inch round bar stock; however, the cavitation damage and tensile test data were not available for the same heat.

As soon as these specimens were machined they were coated with a corrosion protective film \* and stored. This film was removed with methanol before each test. For this initial limited program, only ten specimens were tested for each metal except for SAE 1020 steel for which about 30 specimens were used.

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\* Zip Spray No. 2 by Zip Abrasive Company of Cleveland, Ohio.

Cooling and Environmental Control

Without outside cooling, the fatigue specimens become excessively hot near the node due to the high dynamic strains. To avoid this unwanted heating, a constant temperature, close to atmospheric temperature, was maintained by immersing the specimen in a constant temperature bath. This bath provided simultaneously the corrosive or non-corrosive environment as required. For the present experiments, the fatigue specimens were immersed in a beaker full of either distilled water or methanol, which was kept at constant temperature  $\pm 2^{\circ}\text{F}$ . by means of another cooling jacket through which tap water was circulated. For one set of experiments with SAE 1020 steel, 3 percent NaCl solution was used as the environmental bath to provide the corrosive environment. This arrangement is shown in Figure 6.

RESULTS AND ANALYSIS

Results

Figure 7 shows the results of these tests for five metals, namely:

- (a) 1100-F Aluminum
- (b) 2024-T4 Aluminum
- (c) Tobin Bronze
- (d) Monel
- (e) 316 Stainless Steel.

The dark circles show the results of tests in methanol, whereas all the other tests were conducted in distilled water. These results show the negligible effect of corrosion by distilled water.

Analysis

As pointed out in the introduction, the main aim of these investigations is to obtain a quantitative insight into the strain rate effects on the fracture energy of these metals. The following analysis, originally due to Morrow (3), has been quite useful for this purpose.

Brief review of Morrow's Theory: The following important assumptions are made in this theory.

1. Plastic strain energy is a criterion for finite fatigue life.
2. The total plastic strain energy to fracture increases as the alternating stress is reduced in a completely reversed fatigue test. Specifically, it has been assumed that this quantity is inversely proportional to the fourth power of the alternating stress.
3. The plastic strain energy per cycle can be related to the static true stress-strain curve.

The theoretical justifications, the experimental verification and the limitations of these assumptions are discussed in detail by Morrow in his original paper. The derivation of the essential equations will be touched upon only briefly in this report.

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The plastic strain energy up to fracture per unit volume is given by

$$S_e = \int_0^{\epsilon_f} \sigma d\epsilon_p \quad [8]$$

and

$$\sigma \propto \epsilon_p^n \quad [9]$$

where  $\sigma$  is the true stress corresponding to a true plastic strain of  $\epsilon_p$  (see Figure 8), and  $n$  is the strain hardening exponent.

Now

$$\sigma = \sigma_f' \left( \frac{\epsilon_p}{\epsilon_f} \right)^n \quad [10]$$

where  $\sigma_f'$  is the true fracture stress corresponding to the fracture strain  $\epsilon_f$ . In some materials, deviation from linearity in a log-log plot of true stress versus true strain occurs past necking (probably due to the triaxial stresses present in the necked region). For this reason,  $\sigma_f'$  has been defined as the stress obtained by extrapolating the straight line region as shown in Figure 8(b) to the strain at fracture. The experimentally measured value would be  $\sigma_f$ .

Substituting Equation [10] in [8] and integrating gives

$$S_e = \frac{1}{1+n} \sigma_f' \epsilon_f \quad [11]$$

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Similarly the plastic strain energy, or the work done per cycle  $\Delta w$  is

$$\Delta w = 2 \int_0^{\Delta \epsilon_p} \sigma d \epsilon_p$$

$$= \frac{2}{1+n} \sigma_a \Delta \epsilon_p \quad [12]$$

Assuming that  $\Delta w$  remains constant for the entire test at a given stress level, the work done up to fracture  $W_f$  is given by

$$N_f \Delta w = W_f \quad [13]$$

The dependence of  $W_f$  on  $\sigma_a$  was evaluated by a combination of a dimensional analysis due to Liu (13) and the Griffith crack theory. There is a region of plastic deformation around each crack. Assuming these regions are geometrically similar, the stored plastic energy will depend upon the square of the crack length.

Thus

$$\frac{W_a}{W_1} = \left( \frac{L_a}{L_1} \right)^2 \quad [14]$$

Invoking Griffith's theory,

$$L \sigma^2 = \text{constant} \quad [15]$$

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and hence

$$\frac{L_2}{L_1} = \left( \frac{\sigma_2}{\sigma_1} \right)^{-\frac{1}{n}} \quad [16]$$

Combining Equations [14] and [16], one gets

$$\frac{\sigma_2}{\sigma_1} = \left( \frac{W_2}{W_1} \right)^{-\frac{1}{n}} \quad [17]$$

Hence

$$\frac{\sigma_a}{\sigma_f'} = \left( \frac{W_f}{S_e} \right)^{-\frac{1}{n}} \quad [18]$$

Combining Equations [11], [12], [13] and [18], one obtains

$$2N_f \left( \frac{\sigma_a}{\sigma_f'} \right)^5 \frac{\Delta \epsilon_p}{\epsilon_f} = 1 \quad [19]$$

$$\frac{\Delta \epsilon_p}{\epsilon_f} = \left( \frac{\sigma_a}{\sigma_f'} \right)^{\frac{1}{n}} \quad [20]$$

Now from [19] and [20]

$$\sigma_a = \sigma_f' \left( 2N_f \right)^{-\frac{n}{1+5n}} \quad [21]$$

In logarithmic form

$$\log \sigma_a = \log \sigma_f' - \frac{n}{1+5n} \log (2N_f) \quad [22]$$

Morrow found this analysis for completely reversed, constant amplitude uniaxial fatigue to agree with the trends in forty sets of fatigue data of metals.

The above analysis was used to check the experimental data of the present high frequency fatigue tests. The values of  $\sigma_f'$  and  $n$  as obtained from true stress-strain diagrams for these five metals are shown in Table 2. It was found that Equation [22] fits the experimental data for all of the five metals tested, if the value of  $n$  used in Equation [22] is fifteen percent less than the actual values as obtained from tests. A comparison between the curves predicted from the above analysis using 85 percent of the value of  $n$  and the experimental data are shown in Figure 9. This agreement shows that the high strain rates involved in the present testing method has not substantially changed the plastic energy required to fracture the metal in fatigue. This conclusion is very significant in explaining why the strain energy gives the most significant correlation with cavitation damage resistance.

#### Influence of Corrosion

One of the serious limitations to the above analysis is the influence of corrosive environment. It is known that cavitation damage is greatly increased in a corrosive liquid. For a typical

case of NaCl solutions and SAE 1020 steel, this relationship is reproduced from Reference 7 in Figure 10. It was pointed out in that reference that the estimated electrochemical corrosion could not account for the large increase in damage and therefore the fatigue strength of the metal must have deteriorated due to corrosion. There were some doubts as to whether the fatigue strength could be affected so greatly under such high frequencies. To clarify this point, a few experiments were conducted using SAE 1020 steel. Figure 11 shows the results with methanol, distilled water, and 3 percent NaCl solution as liquid environments. One can easily notice the detrimental effect of corrosion on the fatigue strength of steel even at this high frequency.

An analysis similar to the one above gives the following equation for this steel in a non-corrosive environment.

$$\log \sigma_a = \log 1.25 \times 10^6 - \frac{0.07}{1 + 5 \times 0.07} \log 2N_f \quad [23]$$

The effect of corrosion can be represented quantitatively by means of the following equation.

$$\log \sigma_a = \log \sigma_f' - \frac{n}{1 + 5n} \log 2N_f - CN_f \quad [24]$$

where C is an empirical corrosion fatigue factor. For the present results, n turns out to be  $4 \times 10^{-10}$  as shown in Figure 12. It is believed that a deeper understanding of this corrosion factor C would eventually lead to a quantitative representation of corrosive interaction in cavitation damage.

CONCLUSIONS

Based on the results of these investigations, the following conclusions may be stated.

1. The plastic strain energy correlation found to be successful to represent cavitation damage and low frequency fatigue, can equally be used for correlating high frequency data. This result shows that strain rate effects may not introduce deviations greater than 10 to 20 percent in the strain hardening exponent. This result is significant in explaining the correlations obtained with cavitation damage (1, 2).
2. Fatigue strength of non-resistant metals in a corrosive environment can be significantly changed even under high frequencies. This tends to explain the earlier findings with regard to the very high increase in cavitation erosion in a corrosive liquid (7).

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TABLE 1  
Required Design Parameters for High Frequency  
Fatigue Specimens as Determined Experimentally

Metal	Velocity of Sound fps	Density gms/cm <sup>3</sup>	Modulus of Elasticity psi	Wave Length inches	Modified Wave Length of Notched Specimen (inches)	Resonant Frequency
1020 Mild Steel	16700	7.85	$29.0 \times 10^6$	14.0	13.0	14,290
1100-F Aluminum	16700	2.70	$10.0 \times 10^6$	14.0	13.2	14,210
2024-T <sub>4</sub> Aluminum	16700	2.70	$10.0 \times 10^6$	14.0	13.2	14,200
316 Stainless Steel	16300	7.98	$28.4 \times 10^6$	13.6	12.6	14,220
Monel	14650	8.84	$25.4 \times 10^6$	12.3	11.2	14,300
Tobin Bronze	10950	8.41	$11.8 \times 10^6$	9.2	8.3	14,200

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TABLE 2

The Values Of  $\sigma_f'$  And n For The Five Metals Analyzed

Metal	$\sigma_f'$ Kips	n	85% n	Strain Energy $S_e$ in Kips
316 Stainless Steel	120	0.10	0.085	35
Monel	110	0.08	0.068	24
Tobin Bronze	83	0.10	0.85	17
2024-T4 Aluminum	81	0.13	0.11	13
1100-F Aluminum	26	0.07	0.06	4

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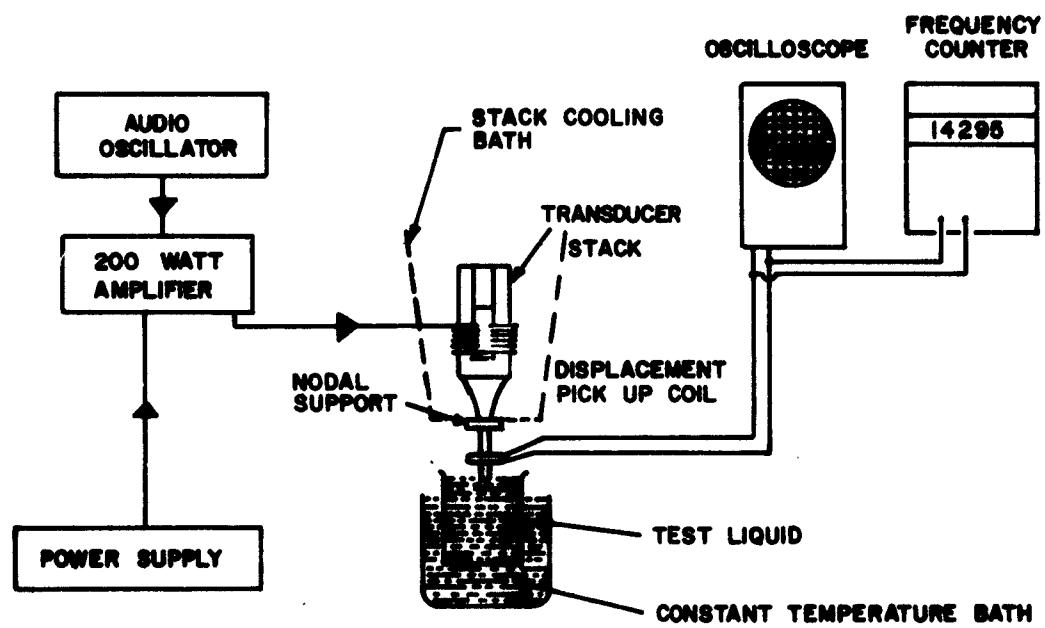


FIGURE 1 - BLOCK DIAGRAM OF THE MAGNETOSTRICTION APPARATUS  
USED FOR HIGH FREQUENCY FATIGUE TESTS

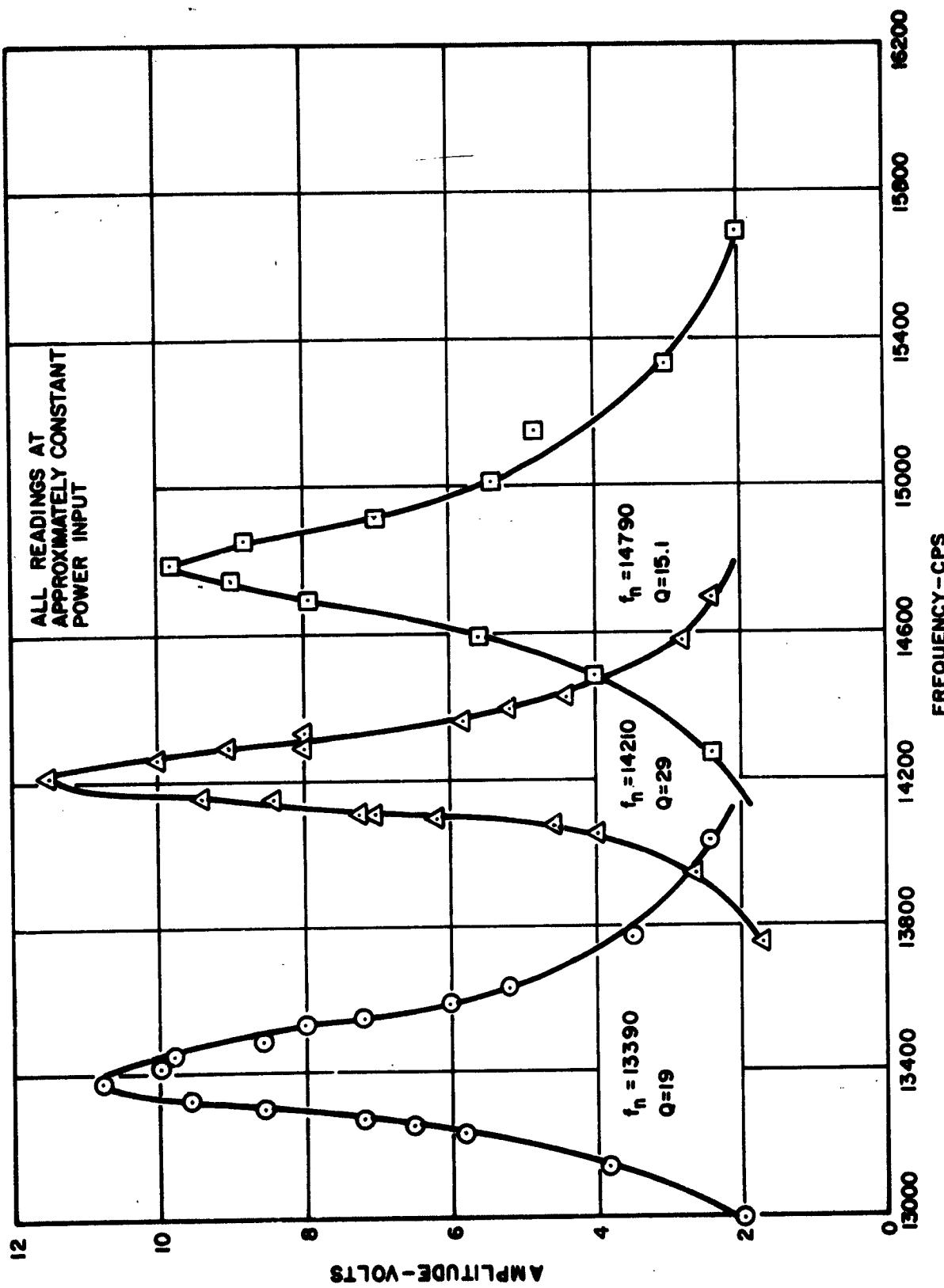
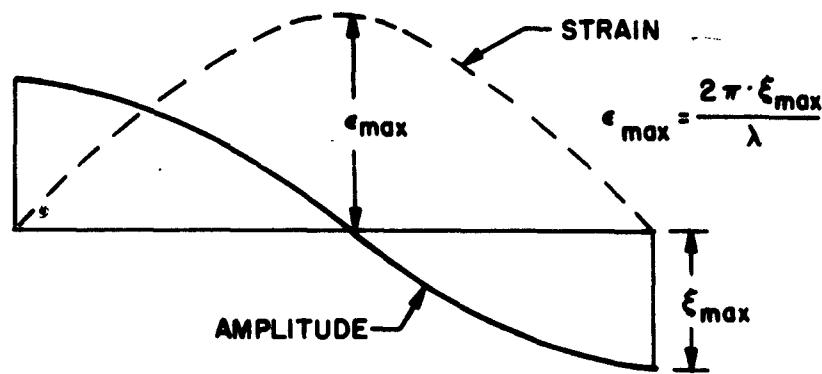
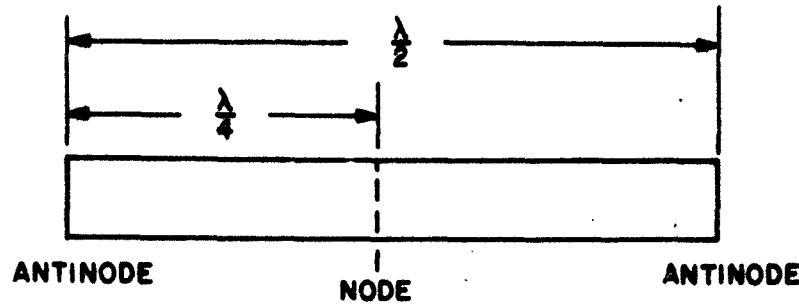
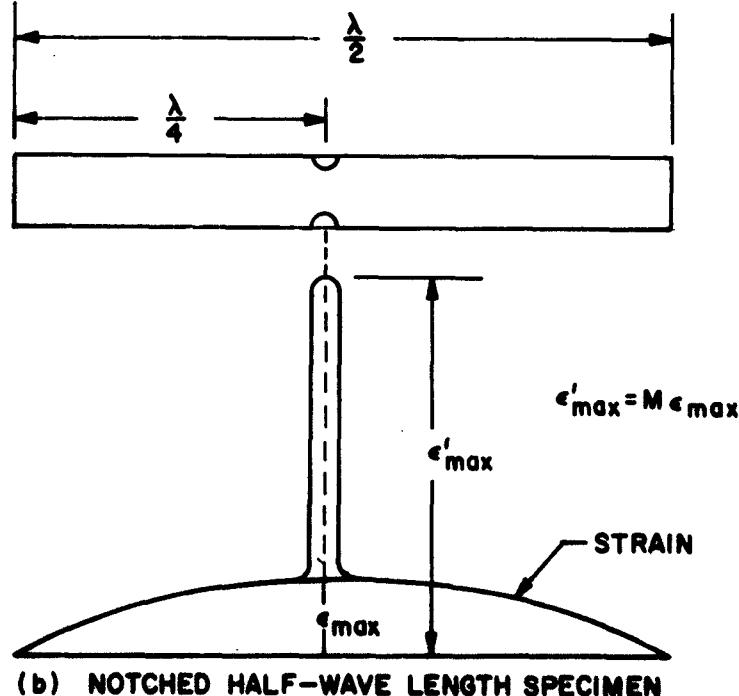


FIGURE 2 - TRANSDUCER CHARACTERISTICS

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(a) UNNOTCHED HALF-WAVE LENGTH SPECIMEN



(b) NOTCHED HALF-WAVE LENGTH SPECIMEN

FIGURE 3 - BASIC PRINCIPLE OF HIGH FREQUENCY FATIGUE SPECIMEN DESIGN

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NOTES:

1. GROOVE (DETAIL "A") IS TO BE SMOOTH, FREE FROM CHATTER, TOOL MARKS, GROOVES OR OTHER DISCONTINUITIES. THE DIMENSIONS OF THE GROOVE MUST BE IDENTICAL FOR ALL SPECIMENS IN A LOT  $\pm .001$  AS MEASURED WITH AN OPTICAL COMPARATOR.
2. FINISH IN GROOVE ~~63~~ OR BETTER
3. DIMENSION "A" = HALF WAVE LENGTH OF SOUND

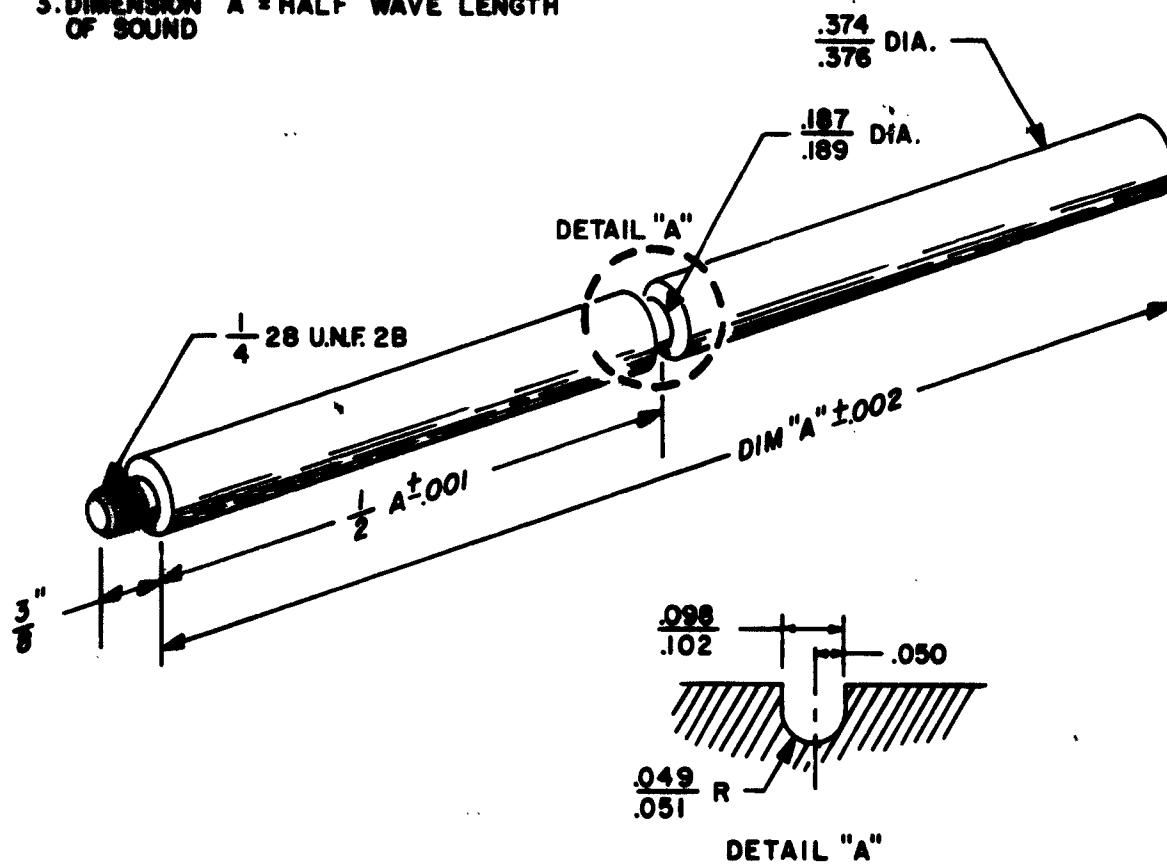


FIGURE 4(a) - HIGH FREQUENCY FATIGUE SPECIMEN

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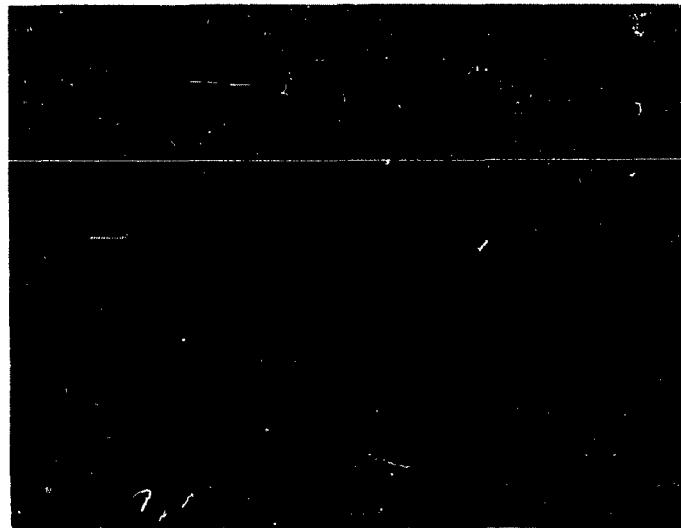


FIGURE 4 (b)-PHOTOGRAPH OF SAE 1020 STEEL FATIGUE SPECIMEN

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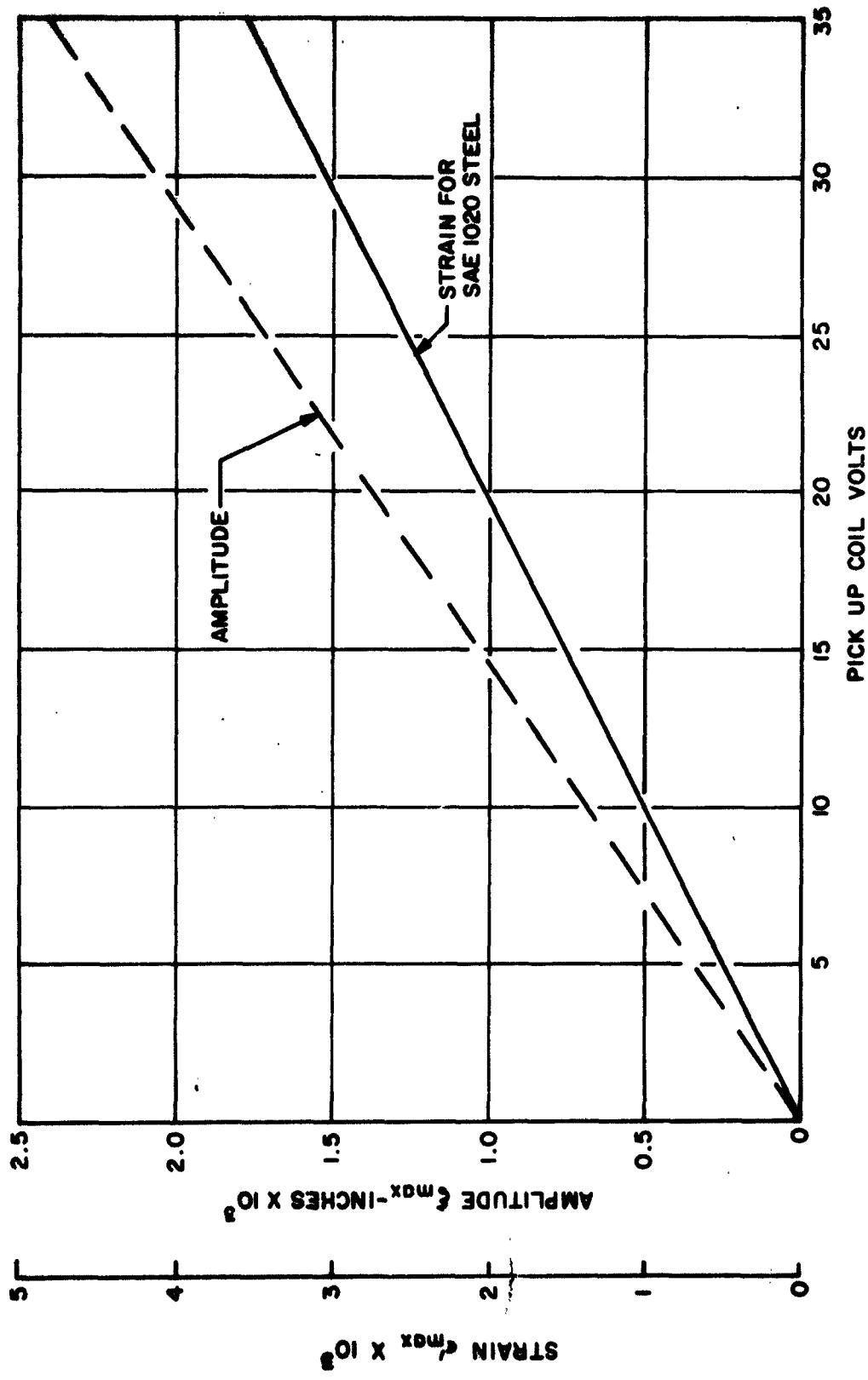
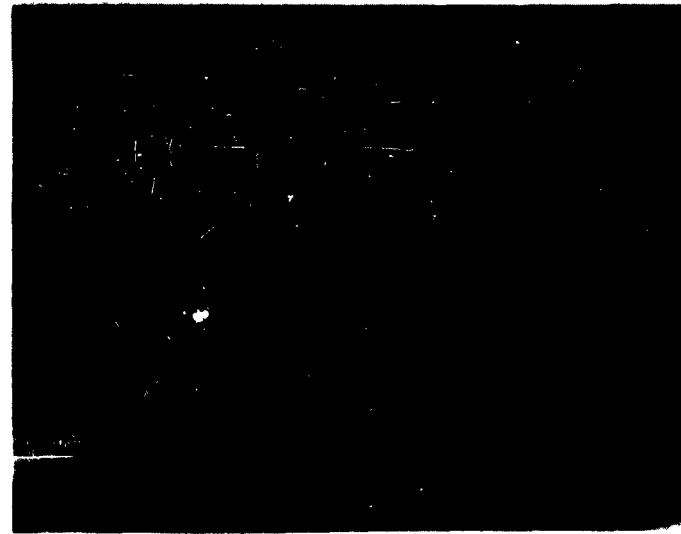
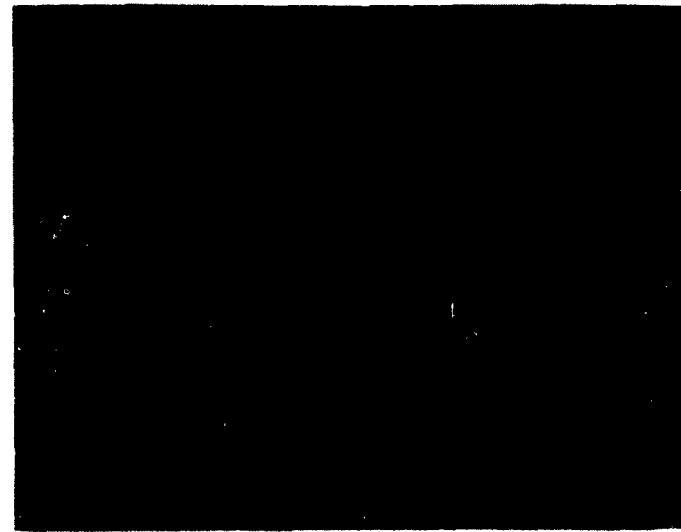


FIGURE 5 - CALIBRATION OF PICK UP COIL FOR MONITORING STRAINS

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(a) OVERALL VIEW



(b) CLOSE UP OF SPECIMEN AND COOLING BATH

FIGURE 6 - GENERAL ARRANGEMENT OF HIGH FREQUENCY FATIGUE TESTING APPARATUS

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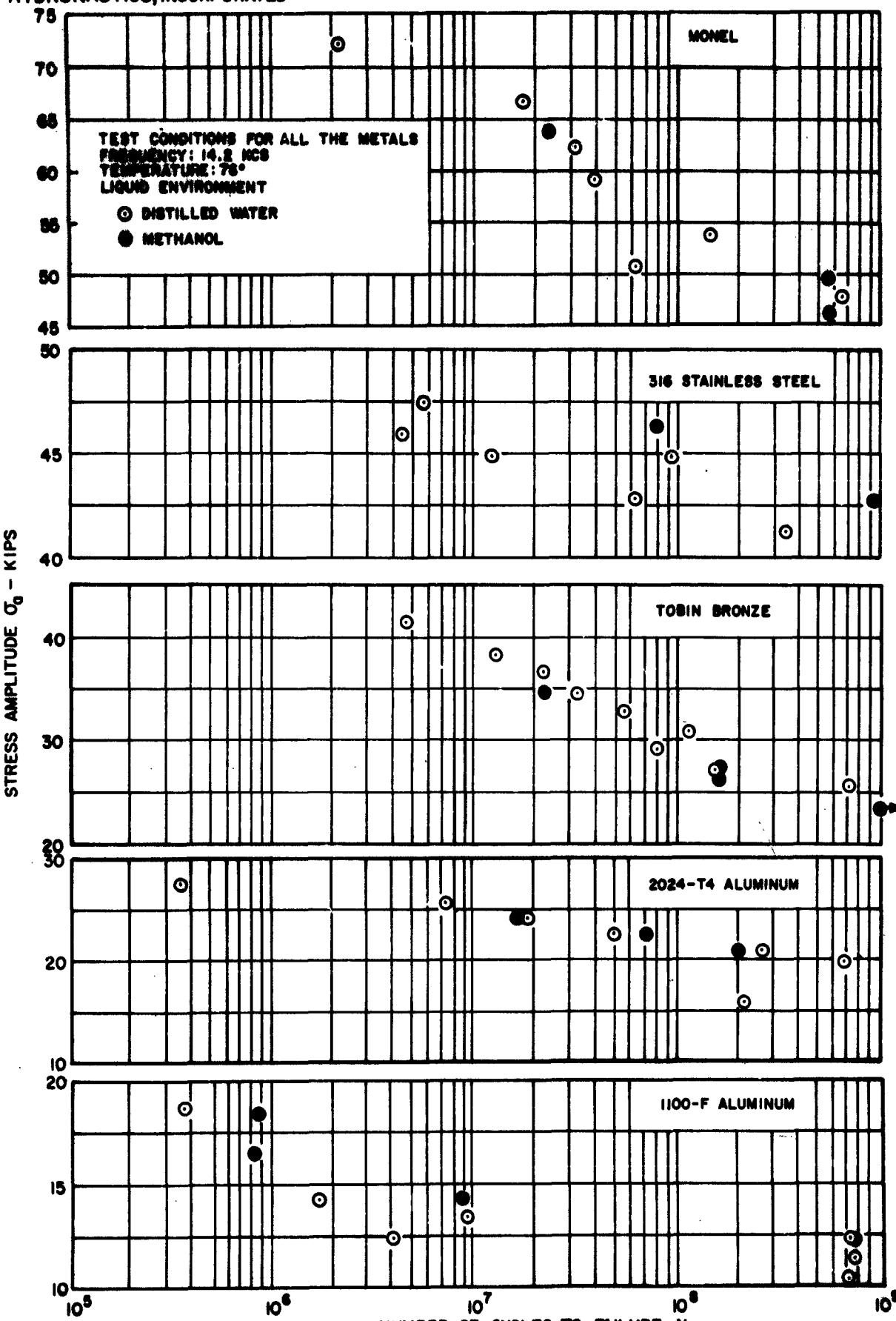
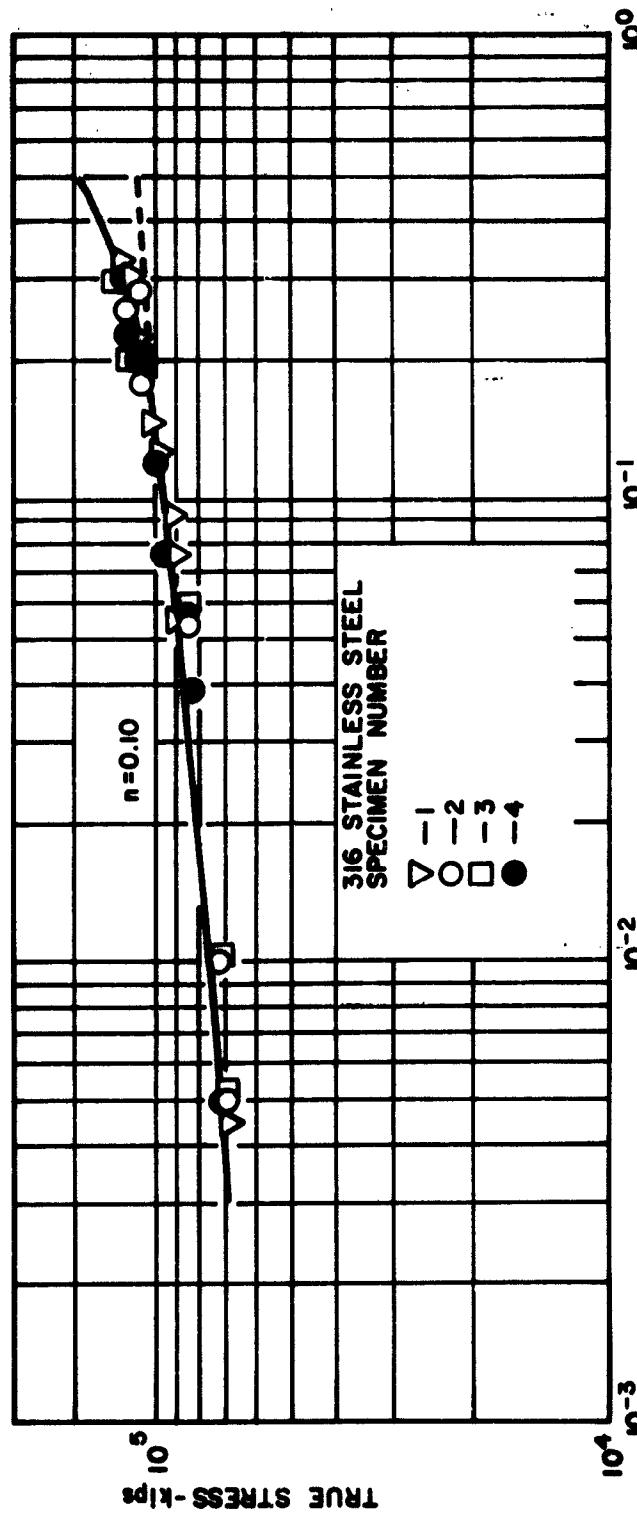
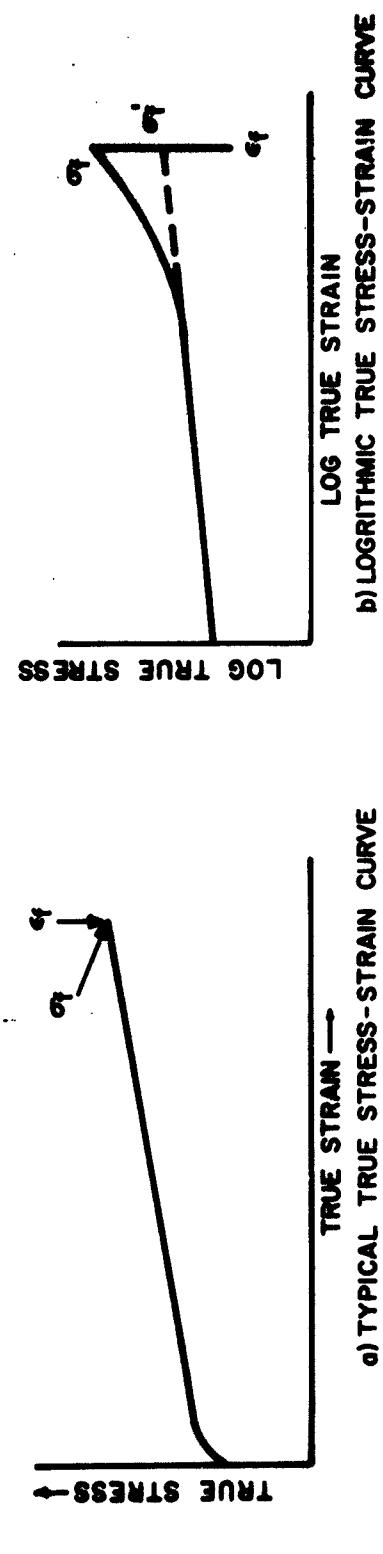


FIGURE 7 - RESULTS OF HIGH FREQUENCY FATIGUE TESTS



c) TRUE STRESS-STRAIN DATA FOR 316 STAINLESS STEEL

FIGURE 8 - TRUE STRESS-STRAIN CURVES

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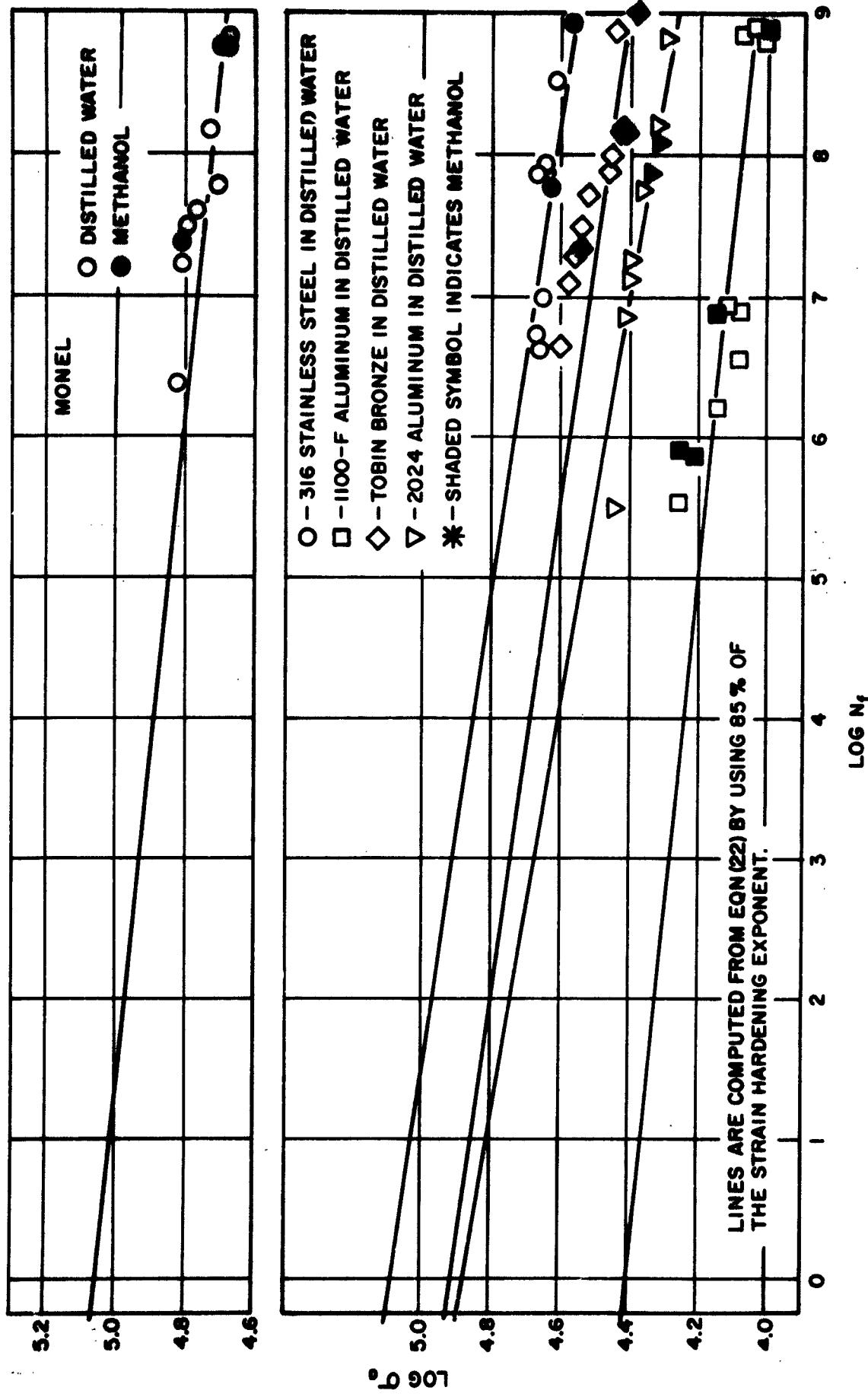


FIGURE 9 - COMPARISON BETWEEN THEORY AND HIGH FREQUENCY FATIGUE DATA

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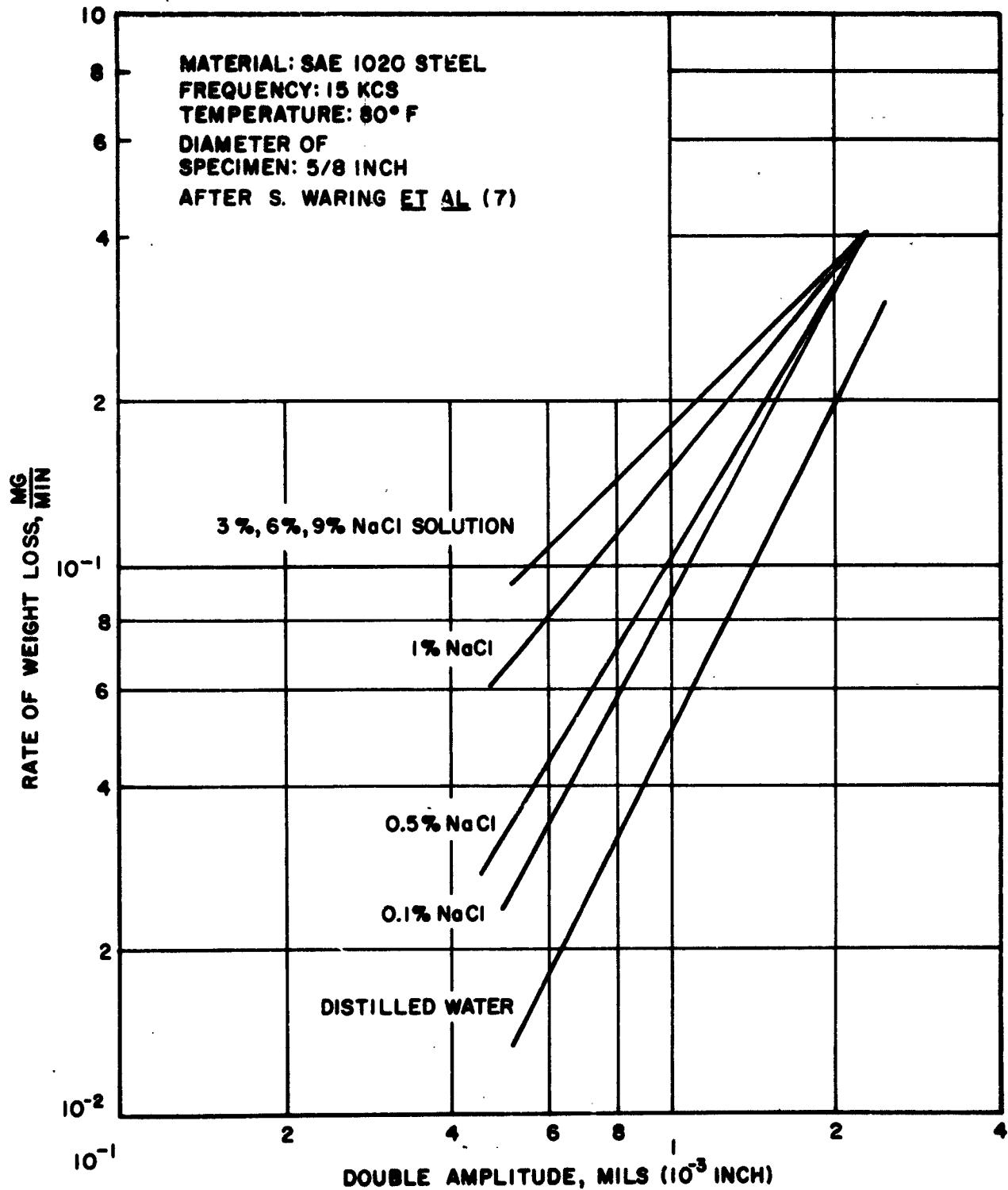


FIGURE 10 -EFFECT OF NaCl CONCENTRATION ON THE AMPLITUDE VERSUS DAMAGE RATE RELATIONSHIP FOR SAE 1020 STEEL

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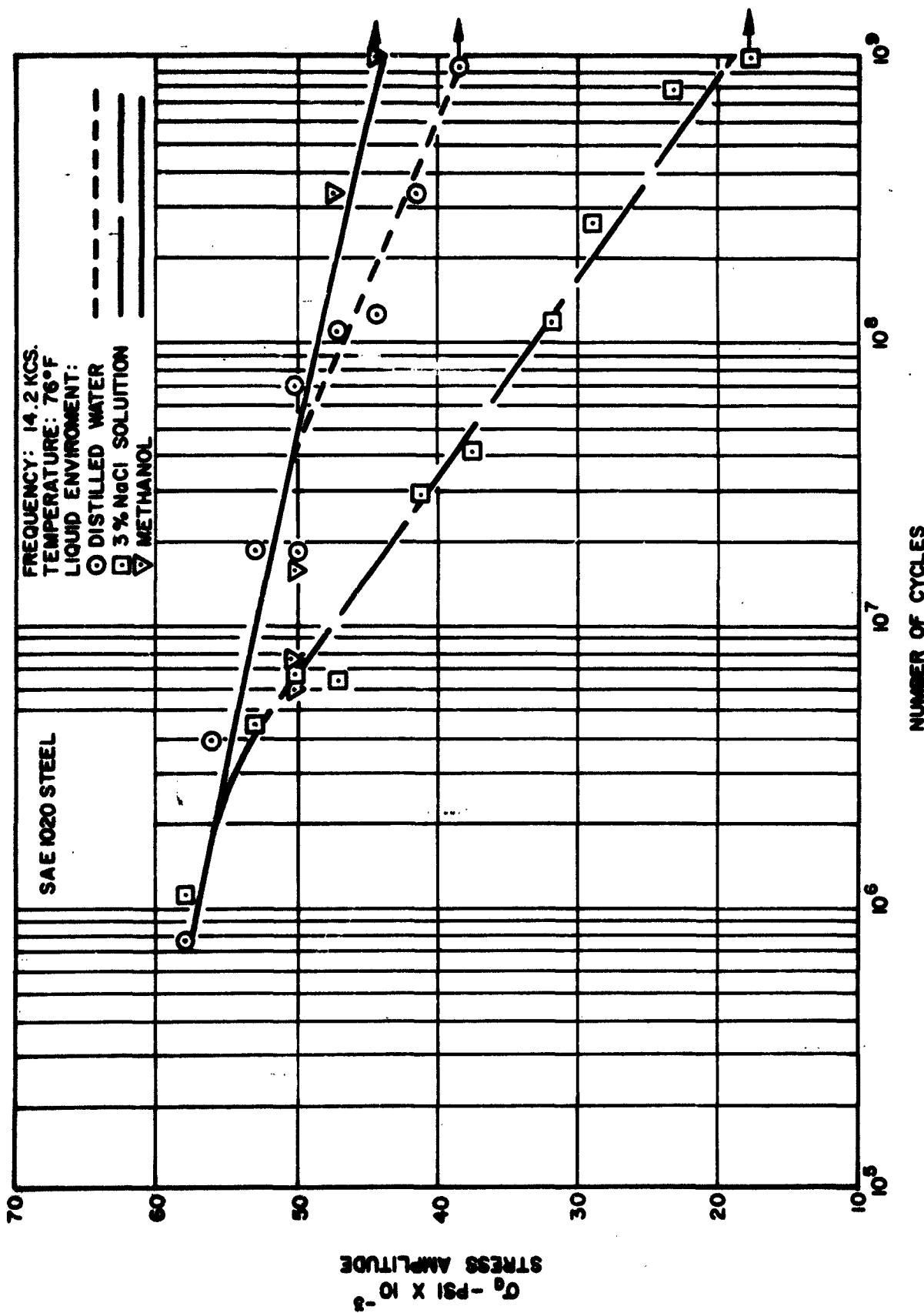


FIGURE II - HIGH FREQUENCY CORROSION FATIGUE OF SAE 1020 STEEL

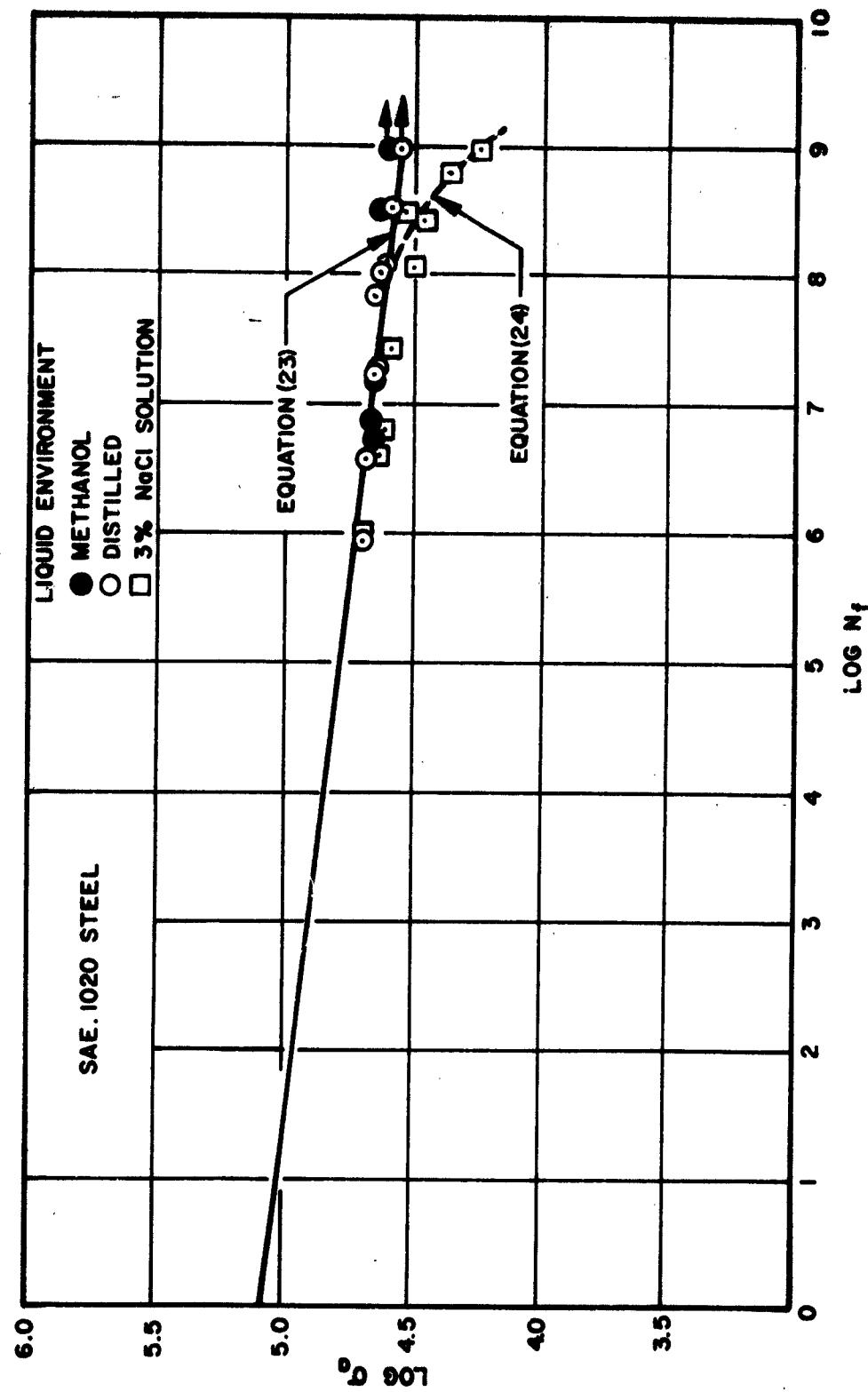


FIGURE 12 - CORROSION FATIGUE OF S.A.E. 1020 STEEL

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5. PRELIMINARY DATA (Type of report and inclusive dates)		
Research Report		
6. AUTHOR(S) (Last name, first name, initial)		
Thiruvengadam, A.		

6. REPORT DATE December 1964	7a. TOTAL NO. OF PAGES 41	7b. NO. OF REFS 13
8a. CONTRACT OR GRANT NO. Nonr 3755(00)FBM, NR 062-293	8b. ORIGINATOR'S REPORT NUMBER(S)	
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In order to verify the strain rate effects on the correlation between strain energy of metals and their cavitation damage resistance, high frequency fatigue tests at 14.2 kcs were conducted using a magnetostriction oscillator. Utilizing Morrow's theory, it has been shown that fatigue at this frequency can be quantitatively predicted if a fifteen percent reduction in static strain hardening factor is made. This result shows that strain rate effects are relatively small when plastic strain energy is used as a criterion.

Another result revealed by this study is the influence of corrosion. Present experiments show that fatigue strength can be reduced significantly for SAE 1020 steel in 3 percent NaCl solution even at high frequencies, thus confirming earlier speculations.

CLASSIFICATION  
Security Classification

14.

KEY WORDS

static fatigue  
high frequency fatigue  
strain energy  
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